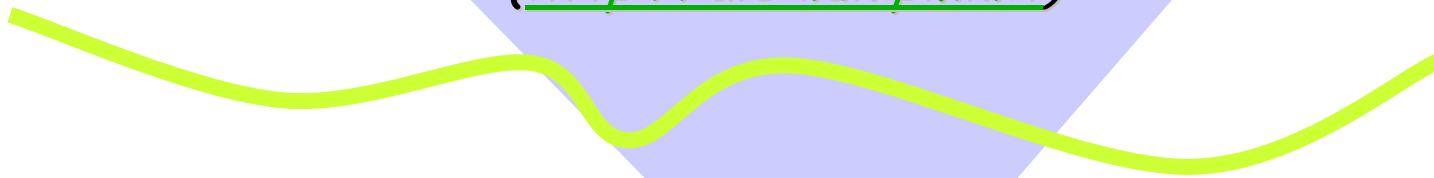


# ALEX4

A simulation program to compare  
electoral systems

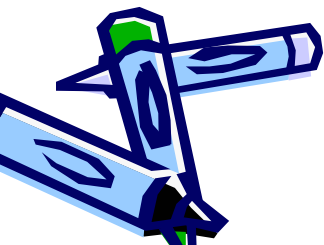
Marie-Edith Bissey, Guido Ortona

*AL.EX - Laboratorio di economia sperimentale e simulativa*  
(<http://alex.unipmn.it>)



# Presentation

- ALEX4 is a cosmetic update of ALEX3.
- A presentation of ALEX3 has been published in
  - M-E. Bissey, M. Carini e G. Ortona, "Alex3: a simulation program to compare electoral systems", Journal of Artificial Societies and Social Simulation, 7, 3, 2004
  - Downloadable from <http://jasss.soc.surrey.ac.uk>
- A general discussion on the simulation of electoral systems is in V. Fragnelli, G. Monella and G. Ortona, "A simulative Approach for Evaluating Electoral Systems", Homo Oeconomicus, 22 (4), 2005



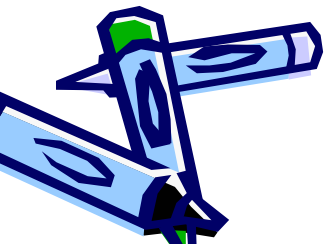
# Why resort to simulation for comparing electoral systems?

- For the comparison to be effective, it is necessary to refer to the same set of *preferences* of the voters. Preferences are *not* proxied by the votes, because votes are affected by the electoral systems.
- The composition of the preferences through an electoral system to produce a parliament is completely *downstream* with reference to the formation of the preferences. Hence a virtual voter is not analogous, but *identical* to a real one. The goodness of the results of the simulation depends entirely on the validity of the simulation program



# Characteristics

- Allows to simulate the preferences of voters and the composition of the districts, according to:
  - The size of the parliament
  - The number of voters
  - The number of parties
  - The size of the electoral districts
  - The weight of the parties in the population
  - The number of electoral districts
  - The size of the plurinominal districts (*optional*)



# Characteristics

- Other parameters can be set:
  - The concentration of the parties in the districts
  - The parameters that are used to create the voters' preference ordering for the parties
  - The parameters that are used to create the voters preference for candidates (for the Single Transferable Vote system)



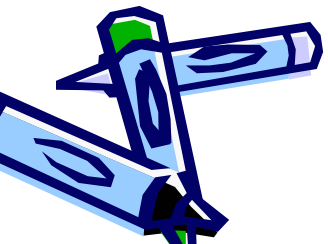
# What the program does

- Given the parameters set up by the user, the program
  - Computes the voters preference order for parties
  - Finds out the composition of the uninominal districts in terms of voters
  - Finds out the composition of the plurinominal districts in terms of uninominal districts
  - Show the resulting parliament according to the system chosen by the user

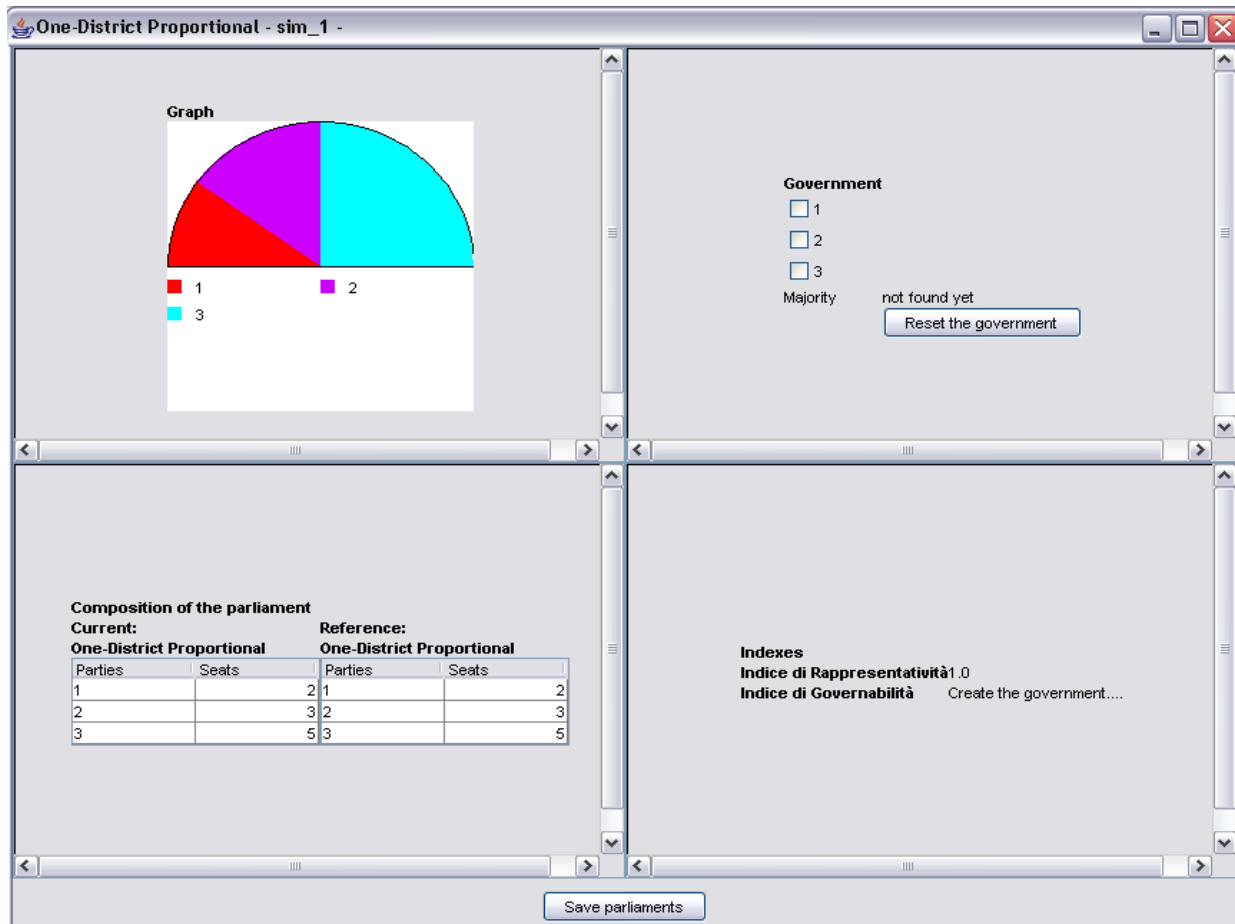


# And now...

- A real example



# The resulting screen





# The electoral systems included in the program

- Borda Criterion
- Condorcet Winner
- First past the Post
- Runoff Majority
- Mixed Member I
- Mixed Member II
- One District Proportional
- Threshold Proportional
- Multi District Proportional
  - D'Hondt
  - Hare
  - Imperiali
  - Droop
- Single Transferable Vote
  - Droop
  - Hare
  - N.B.
- VAP



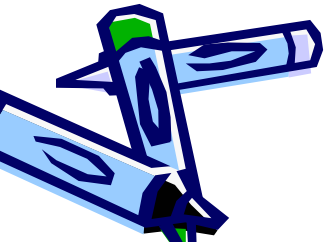
# The following will be added soon

- Approval
- Multi District Threshold Proportional
- Majority Premium



# Output of the program

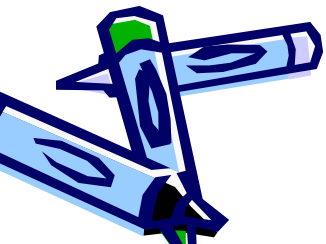
- The composition of the parliament
- An index of representativeness
- An index of governability



# The representativeness index

- The index of representativeness for electoral system  $j$  is

$$r_j = 1 - (\sum |S_{j,i} - S_{pp,i}|) / (\sum |S_{wta,i} - S_{pp,i}|)$$



# The representativeness index

$$r_j = 1 - (\sum |S_{j,i} - S_{pp,i}|) / (\sum |S_{wta,i} - S_{pp,i}|)$$

- *First sum:* The loss of representativeness incurred by party  $i$  is the (absolute) difference between the seats it would get under PPR and those actually obtained. Summing losses across all parties we obtain the total loss of representativeness.

# The representativeness index

$$r_j = 1 - (\sum |S_{j,i} - S_{pp,i}|) / (\sum |S_{wta,i} - S_{pp,i}|)$$

- To be normalized (0 to 1), the total loss of representativeness is divided by the *maximum possible loss*. This maximum is obtained when "winner takes all" in a very strict sense, that is when the relative majority party takes all the seats.

# The representativeness index

$$r_j = 1 - (\sum |S_{j,i} - S_{pp,i}|) / (\sum |S_{wta,i} - S_{pp,i}|)$$

- *1-the ratio of the sums: up to now we got a loss of representativeness index, normalized in the range 0-1. Subtracting it from 1 we transform it into a representativeness index.*

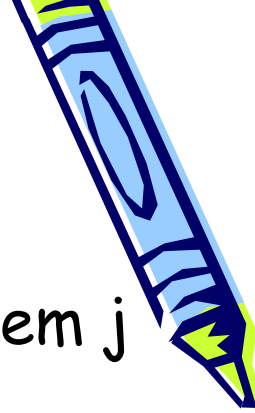


# The index of governability

- The index of governability for electoral system  $j$  is

$$g = g_m + g_f$$

- It is made of two components, added lexicographically. The first and more important,  $g_m$ , refers to the *number of parties of the governing coalition*; the second,  $g_f$ , to the *number of seats of the governing coalition*.





# The index of governability

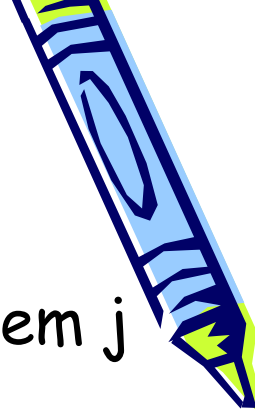
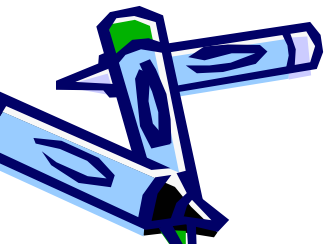
- The index of governability for electoral system  $j$  is

$$g = g_m + g_f$$

- First component:

$$g_m = 1/(m+1)$$

- $m$  = number of parties great enough for the government to lose the majority if they withdraw.



# The index of governability

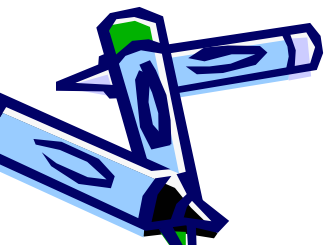
- The index of governability for electoral system  $j$  is

$$g = g_m + g_f$$

- Second component:

$$g_f = 2(f - 0.5) * [1/m - 1/(m+1)]$$

- $f$  = share of seats of the majority
- $g_f$  tends to 0 if the majority is of just 1 seat, in which case  $g$  tends to  $1/(m+1)$ , and is equal to  $1/m - 1/(m+1)$  if the majority has all the seats, in which case  $g = 1/m$



# Other characteristics of the program

- It is possible to save all the data of the simulation
  - Initial parameters
  - Voters' preferences for the parties, the candidates
  - Composition of the uninominal and the plurinominal districts
  - Simulated parliament
- It is possible to import these data in the program
- It is possible to recreate these data (e.g. from surveys) to simulate parliaments using real data.



# Other characteristics of the program

- It is written in Java and will run on any operating system
- Multilingual: so far it exists in
  - Italian
  - English
  - French
- Adding another language only requires the translation of some text files, no further programming is involved.



# Uses of the program

- Confront the existing electoral systems to see for instance how in any given situation the system is use performs with respect to possible alternatives
- Search for the best electoral system in a given situation
- Find out how a new electoral system may perform with respect to existing systems.



# Some results obtained with alex4 or its ancestors



*numbers are of working papers of dep. POLIS of this university*

- **60**: Under plausible conditions, the mixed system employed in Italy in the last decade was dominated either by proportionality or plurality; the present one may be the best one, but it is unlikely
- **47**: An experiment on the choice of the electoral system by the electors produced the Condorcet system as the best one
- **32**: An Italian-like case with the preferences of the end of the 90s suggest that proportional systems are preferable, but there are hints that the sensitivity is very high.
- **4**: Assessment of a new system, successful.



# Publications using ALEX3 and ALEX4

- <http://jasss.soc.surrey.co.uk>
  - This paper presents the program (in its previous version), simulates and confronts some electoral systems for the case of Italy and the United Kingdom.
- <http://polis.unipmn.it/pubbl/>
  - W.P. n. 4 - evaluation of new electoral systems
  - W.P. n. 32, 38, 47 e 60 - choosing the best electoral system



# Scaricare il programma

- [beta version]  
<http://alex.unipmn.it/activities/ALEX4.zip>
- The program is freeware, we only ask for the authors who use it to say so in their papers ...
- and to send us a copy of the paper!
- For further information, please write to [guido.ortona@sp.unipmn.it](mailto:guido.ortona@sp.unipmn.it) (theoretical matters) or [marieedith.bisseey@sp.unipmn.it](mailto:marieedith.bisseey@sp.unipmn.it) (whatever has to do with the program itself)

